CS 331, Fall 2025 Today! - Kevin's research

- Fine-grained composity

Lecture 26 (1218)

- Popular conjectures

leun's research

Algorithmic princitives for "big" data science

= 1/2: continuous algos foundations (opt, samp, NLA)

7 1/2: trustworthy ML (robustness, proscy, farness)

ley themes:

- · Many problems had in worst case. Harness structure.
- · Where does the data come from? Minimal assumptions.
- · Dataset sizes enurous, only growns. Nex-lines time?

Trustworthy ML

Textbook setting for statistics/leaning:

$$X_1=($$
 $X_2=($
 $X_3=($
 $X_3=$

- · What if we're wrong about the data? Folustiness
- . The data is combs from humans. Privacy/fairness
- . Why do we believe the model's conclusion? Interpretability
- ... all needs to happen efficiently...

Continuous 2 lyos

What kind of tools are useful for movern algo design?

OPT: Minimize structured objectives.

C.S. Minimax (Stochastic Opthi-Zatur Semidefhite programmus ("matrix LP") Strutured nonconvex prodems (Sparty, GLM,...)

SAMP: Sample from Structured desties.

e.s. loguerous sampling (basic tractable family)
Strutured nulthrodal problems

NLA: numerical lines algebra primitives

e.g. preconditioning (soluts linear systems, repression)

Sparitistion (replie data will representatives)

2014: Google Intenship. Not good at it ...

2015: Complexity research. Not you at it...

2016: Genonics research. Peally fun! 1 like alsos best ...

2017: Geronics/NLP/Stats research. (Ph.D. rotaturs)

7018: Apprehise maxtlew.

20(9: Nah equilibria, orthod trasport, SDP.

2020: Sampling. SOTA for some logionere families.

2021: Poloust Stats. P(A, regression, clusterly in wear-liverture.

2022-25: Privacy, interpretability, fames, etc.

I In types to leave more about more ML.

Algorithms are cool and come in many flavors. There are so many connections. Just keep learning and every in

More TCS @ UT!

(S 353: Theory of Computation
(a second course in complexity)

Craduste algos courses

(S 388E: Approximation (S388R)

(5389C: Conthuous

CS388R: Radonited

CS 390S: Sublineur

29chos Lexalmos arrocal

CS 388T: Camplicity theory

CS 388 M: Communication

Must else?

CS 346/388H: Cryptography

CS 358H/378H: Quartum information

topics (12)362

Thinks to: Virguis Williams (notes) Amir Abbaud } Knowle Hick fisher Fire-graned Conplexity So far: Complexity theory for "small 1272" N = [00], 000, [000] = N"N20" not polyther: SAT pulytine: Sort / search (we think) Vertexlover 3r.thmetic Knapsalk lines algebra TSP Strings Mxwt Lrachspilly APSP Sudoku It's 2025. We need comprexity theory for "big data" n= 109, 1018, 1015...

lexy" "nedwn" "had"

tine floor paythe hot paythe

the her-liver

W.	3	twol	to	your	yrddems	M3r8
(1	J	1301	• -	,	1	

Today: how to move problems medium.

Enoun essy

FFT

Shortest path

Maxflow

Longest moressly subseq.

Closect pair in P2

Longest palhonomic substitus

Suspected medium

3-SUM

All-pairs Sharterit parks

Dynamic maxiflow

Longest common subseq.

(Losest par in R

(Josest par in R

(Josest par in R

(Josest par in R

e-5. APSP N3 ... N3-ou)
Floyd-Washall '62 Williams '14

Why are we so good at problems on LHS?

Good in FGC: heb of reductors, common source of hardness
must attack first!

Popular Conjectures
let E>O be Small constant.
3-SUM: Given list L & #'s,] 2, b, CEL
S.t. 2+b+c=0?
cannot be solved in time O(L 2-2)
APSP: Given graph (= (ViE, w) compute
Ul x [V] matrix enacts 211-yours shortest paths
Canot be solved in the O(1V13-E)
SETH: 7 constant K S.t. K-SAT ON

Rough intuition: we are about the exponent how.

3-50M

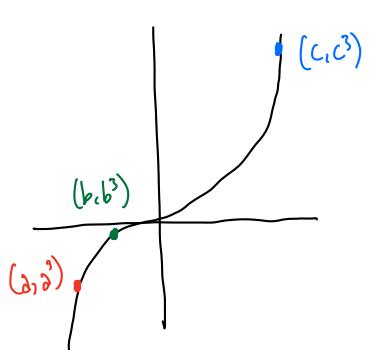
Computational geometers Gajentaan - Overnous 195 Kick off field of FGC by reducing to 3-SUM.

Example: Collinearity requires and time.

Input: n points in R? . I three on a live?

(This proof is uszy.) Reduce 3-50M to colliering.

Check collinsing ({(x, x3) | x E L})



$$\frac{b^{3}-a^{3}}{b-a} = \frac{2^{3}-b^{3}}{c-b}$$

$$\frac{2^{4}+2b+b^{2}}{2^{2}-c^{2}} = b(c-a)$$

$$-3-c=b \quad (3-SUM)$$

More: Visibility (reschability)

Several require

ingenery to solve in = u2.

APSP

This is really about "Combinatoria" motrix multiplication.

Many amazins "2/jebraic" imovatins:

(nxn) (nxn) takes the ...

multiply

N^{2.807} Strassen :

N 2.3714 ADWXXZ

Use crazy cancellations on huse tensors...

What if we can only use more "boseline" techniques?

product -> Sum

DPL-1 = DPL HLE (O(los (us)))
"Min-plus" another

To solve APSP, need to solve combinatorial maximal Ollog(n) thes. Thus, APSP consecture:

Combinatorial maternal needs and time is

Good news: Structured maternal / merson / ... easier!

SETH

Perall 3-SAT solvable in: $O(2^n m)$ time Improvement: Try 7/8 for one clause, recurse. The 7/18 for one clause, recurse. $T(n) \leq 7T(n-3) + O(m) \Rightarrow T(n) = O(1.913^n m)$

So, 3-SAT does not need 2" time.

More general: K-SAT in 2" (1-octs) on time.

But we need tight base (w:11 later choose n = los)
base becomes exponent.

Herce SETH: Choose large enough K.

Almost all movern reductions use SETH thru:

SETH & OV (orthogon) vectors)

Williams, 2005

OV implies FGC of so many problems:

· Diameter

· 604 1xx

· Loul aliment

· Dynamic resubsility

· Frêdet distance

· Stable matching

. Shyle-sarce mixflow

· LLS

· Usest yar

1200 problem: let d= w(logur) "spasse subset" A, B C {OII}, size n 7 aet, bes st. 27 b = 0? orthymal Conjecture: no better than = n2d possible. K-OV: there we K sets A, A2 A3 ... C \ 0,138 70,6A1, 226 A21 236 A31... s.t. 7 a,[i] 2,(i) 2,(i) ... =0? (6(1)

Conj: needs = ntd fine.

Obs 1: 2-0V is very fundamental. FGC! Obs 2: 2-0U 3 3-0V2... 7 K-0V. Obs 3: "OV 7 SETH". Suppose there's k-OU in O(NKU-E). Take K-SAT formula D, M Variables m chases Creste A1,..., Ax C {0113m: $X \in \{0113^N \rightarrow \{X_1 \mid X_2 \mid ... \mid X_k\}$ $X \in \{0113^N \rightarrow \{X_1 \mid X_2 \mid ... \mid X_k\}$ W/K W/K W/K

A: = index by $N = 2^{n/k}$ assignments to ith block Faster =) SAT in time $N \times (1-\epsilon) = 2^{n(1-\epsilon)}$ (violates SETH!)